### Inquisitive and alternative semantics

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#### Workshop on alternative-based semantics



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www.illc.uva.nl/inquisitive-semantics

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#### Inquisitive semantics

AnderBois, Balogh, Ciardelli, Groenendijk, Haida, Kaufmann, Mameni, Mascarenhas, Pruitt, Roelofsen, Sano, van Gool, a.o.

#### Alternative semantics

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Aloni, Alonso-Ovalle, Kratzer, Menendez-Benito, Shimoyama, Simons, Rawlins, a.o.

Commonalities? Differences?

Notational variants? Competing theories? Complementary efforts?

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## Commonalities Differences

Notational variants? Competing theories? Complementary efforts

# Overview

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### Bird's eye view

- Commonalities
- Differences

#### Street view

- Inquisitive semantics as a semantic framework
- Repercussions for logic
- Repercussions for pragmatics

### Final remarks

From framework to theories

# Bird's eye view



## Commonalities

#### Formal machinery

• The formal machinery developed by both frameworks makes essential use of alternatives.

#### **Empirical focus**

• Theories that are based on alternative or inquisitive semantics often focus on a similar range of linguistic constructions, namely those that are taken to 'introduce alternatives': interrogatives, disjunction, indefinites, indeterminate pronouns.

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### First difference

#### Purposes

- The main purpose of alternative semantics is to facilitate a compositional semantics of constructions involving indefinites/disjunction/indeterminate pronouns.
- The main purpose of inquisitive semantics is to develop a new notion of semantic meaning, which does not only embody informative content, but also inquisitive (and attentive) content.

## Second difference

#### Improvement vs enrichment

- Alternative semantics makes previous theories better at doing what they were always intended to do: deriving the truth-conditions / context change potential of a sentence in a compositional way
- Inquisitive semantics enriches previous frameworks: it allows formal semantic theories to capture aspects of meaning that previous theories were never even *intended* to capture

## Second difference

#### Improvement vs enrichment

- Alternative semantics makes previous theories better at doing what they were always intended to do: deriving the truth-conditions / context change potential of a sentence in a compositional way
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Compare:

- From extensional to intensional semantics
- From static to dynamic semantics

# Third difference

#### Repercussions

- Inquisitive semantics enriches the notion of semantic meaning
- This gives rise to a richer pragmatics as well
  - Maxims concerned with informative content, but also with inquisitive and attentive content
- It also leads to a richer logic
  - Informative, inquisitive, and hybrid notions of entailment
  - Logical notions of relatedness, e.g. compliance
- Alternative semantics leaves the notion of meaning in tact. As such, it has no direct repercussions for pragmatics or logic.

# Summary

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#### Commonalities

- alternative-based formal machinery
- similar empirical focus

#### Differences

- completely different purposes
- improve vs enrich
- repercussions for logic and pragmatics

## Street view



# Street view

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#### Semantics

- Propositions as proposals
- Projection operators
- Algebraic operators

### Logic

- Informative, inquisitive, and hybrid entailment
- Compliance

### Pragmatics

- Sincerity
- Transparency
- Relation

- Meaning = informative content
- Providing information = eliminating possible worlds



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- Captures only one type of language use: providing information
- Does not reflect the cooperative nature of communication

- Propositions as proposals
- A proposal consists of one or more possibilities
- An inquisitive proposal offers several alternative possibilities



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## Worlds, possibilities, and propositions

- Start with a universe of possible worlds
- Possibility: set of possible worlds
- Proposition: set of possibilities

### Illustration



## Information, issues, and attention



A proposition  $\pi$ :

- draws attention to all the possibilities in  $\pi$
- provides the information that at least one of these possibilities contains the actual world
- requests enough information to establish for at least one of these possibilities that it indeed contains the actual world

## Information, issues, and attention



A proposition  $\pi$ :

- draws attention to all the possibilities in  $\pi$
- provides the information that at least one of these possibilities contains the actual world
- requests enough information to establish for at least one of these possibilities that it indeed contains the actual world

 $\Rightarrow$  a single semantic object captures attentive, informative, and inquisitive content all at once

## Alternative and residual possibilities



- Providing the information that at least one of {α, β, γ} contains the actual world is the same as providing the information that at least one of {α, β} contains the actual world
- Requesting enough information to establish at least one of {α, β, γ} is the same as requesting enough information to establish at least one of {α, β}
- So: as long as we are only interested in capturing informative and inquisitive content, γ is irrelevant

## Alternative and residual possibilities



- In generally, for any proposition  $\pi$ , we distinguish:
- Residual possibilities
  - properly contained in a maximal possibility in  $\pi$
  - only play a role in capturing attentive content
- Alternative possibilities
  - not properly contained in a maximal possibility in π
  - completely determine informative and inquisitive content

## Informative content



- A proposition π provides the information that the actual world is contained in at least one of the possibilities in π
- So, the informative content of π, info(π), is determined by the union of all the possibilities in π:

$$info(\pi) = \bigcup \pi$$

## Informative content



- A proposition *π* provides the information that the actual world is contained in at least one of the possibilities in *π*
- So, the informative content of π, info(π), is determined by the union of all the possibilities in π:

$$info(\pi) = \bigcup \pi$$

## Informative, inquisitive, and attentive propositions

- π is informative iff it proposes to eliminate at least one world
- $\pi$  is inquisitive iff it offers at least two alternative possibilities
- $\pi$  is attentive iff it contains at least one residual possibility



## Interlude: relevance for natural language semantics





### Back to propositions in abstracto: projections



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### Projections onto the axes



 $[!]\pi$ purely informative projection $[?]\pi$ purely inquisitive projection $[\diamondsuit]\pi$ purely attentive projection

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### Projections onto the planes



 $[?\diamondsuit] \pi$ non-informative projection $[!\diamondsuit] \pi$ non-inquisitive projection $[?!] \pi$ non-attentive projection

# Example: purely informative projection

### Requirements

- $[!]\pi$  should preserve the informative content of  $\pi$
- $[!]\pi$  should be non-inquisitive
- $[!]\pi$  should be non-attentive

### Implementation

• 
$$[!]\pi = \{\bigcup \pi\}$$



# Example: purely informative projection

### Requirements

- $[!]\pi$  should preserve the informative content of  $\pi$
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#### Implementation

•  $[!]\pi = \{\bigcup \pi\}$ 



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 $\approx$  'existential closure' in alternative semantics

# Another example: non-inquisitive projection

### Requirements

- $[!\diamond]\pi$  should preserve the informative content of  $\pi$
- $[!\diamond]\pi$  should be non-inquisitive
- $[! \diamond] \pi$  should preserve the attentive content of  $\pi$

### Implementation

• 
$$[!\diamondsuit]\pi = \pi \cup \{\bigcup \pi\}$$



## Interlude: relevance for natural language semantics

- It makes sense to think of [!◊] as the semantic contribution of declarative complementizers
- Earlier examples:
- (4) John is in London or he is not in London.
- (5) Mary is in Paris or she is not in Paris.





## Ordering propositions, join and meet

### Classically

- · Propositions are ordered in terms of informative content
- $\pi \ge \pi'$  iff  $\pi$  provides at least as much information as  $\pi'$
- Formally:  $\pi \ge \pi' \iff \pi \subseteq \pi'$

### Join and meet

- Relative to ≥, every two classical propositions have
  - a greatest lower bound (aka their meet)
  - a least upper bound (aka their join)
- The meet of two propositions amounts to their union
- The join of two propositions amounts to their intersection
- Disjunction and conjunction are usually seen as the syntactic counterparts of these semantic operations

## Ordering propositions in inquisitive semantics

- In inquisitive semantics, propositions can be ordered in terms of their informative content, but also in terms of their inquisitive or attentive content, or a combination thereof
- We focus here on the case where propositions are only intended to capture informative and inquisitive content
- In this setting, propositions are sets of alternative possibilities
- The order between them has an informative and an inquisitive component

## Ordering propositions

- $\pi \ge_{info} \pi'$  iff  $\pi$  provides at least as much information as  $\pi'$ : info $(\pi) \subseteq info(\pi')$
- $\pi \ge_{inq} \pi'$  iff  $\pi$  requests at least as much information as  $\pi'$ :

$$\forall \alpha \in \pi. \exists \beta \in \pi'. \alpha \cap \mathsf{info}(\pi') \subseteq \beta$$

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•  $\pi \ge \pi'$  if and only if  $\pi \ge_{info} \pi'$  and  $\pi \ge_{ing} \pi'$ 

### Join and meet

- As before, relative to ≥, every two propositions have
  - a greatest lower bound (aka their meet)
  - a least upper bound (aka their join)
- To determine the meet of two propositions, we first take their union, and then filter out residual possibilities:

$$\texttt{meet}(\pi,\pi')=\texttt{alt}(\pi\cup\pi')$$

• To determine the join of two propositions, we first take their pointwise intersection (denoted by □), and then filter out residual possibilities:

$$\mathsf{JOIN}(\pi,\pi') = \mathsf{ALT}(\pi \sqcap \pi')$$

• Disjunction and conjunction can still be seen as the syntactic counterparts of these semantic operations

# $\langle \Sigma, \ge \rangle$ is not a Boolean algebra

- The existence of meets and joins implies that the set of all propositions Σ, together with the order ≥, forms a lattice
- Moreover, Σ has:
  - a smallest element,  $\top = \{W\}$
  - a greatest element,  $\bot = \{\emptyset\}$
- This means that  $\langle \Sigma, \ge \rangle$  forms a bounded lattice
- However, notably,  $\langle \Sigma, \ge \rangle$  does not form a Boolean algebra
- That is, not every  $\pi \in \Sigma$  has a complement  $\pi'$  such that:

$$ext{MEET}(\pi,\pi') = op$$
  
 $ext{JOIN}(\pi,\pi') = op$ 

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# $\langle \Sigma, \ge \rangle$ is a Heyting algebra

- We do have that for every two propositions π, π' there is a unique minimal element δ of Σ such that Join(π, δ) = π'
- This element δ is called the relative pseudo-complement of π with respect to π', and is denoted as:

#### $\pi \Rightarrow \pi'$

- The existence of relative pseudo-complements implies that (Σ, ≥) forms a Heyting algebra
- The (non-relative) pseudo-complement of  $\pi$  is defined as:

 $\sim \pi \coloneqq \pi \Rightarrow \bot$ 

 Implication and negation could be seen as the syntactic counterparts of ⇒ and ~, respectively

### Intermediate conclusions

- The main purpose of inquisitive semantics is to offer a new notion of semantic meaning: propositions as proposals
- This new type of propositions can be studied from a purely semantic perspective—without reference to any formal or natural language
- This gives rise to projection operators like [?] and [!], and algebraic operators like JOIN, MEET, ⇒, and ~
- Complementizers and connectives in formal and natural languages could be seen as syntactic counterparts of these semantic operators

# Logic

### Traditionally

- logic is concerned with entailment and (in)consistency
- given these concerns, it makes sense to identify semantic meaning with informative content

#### Vice versa

- if semantic meaning is identified with informative content, and propositions are construed as sets of possible worlds
- then there are only three possible relations between two propositions: inclusion, overlap, and disjointness
- these correspond to entailment and (in)consistency
- other relations between propositions cannot be captured

## Entailment and (in)consistency

If propositions are construed as sets of possible worlds then two propositions can only be related in one of the following three ways



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# Inquisitive logic

#### A new perspective

 Enriching the notion of semantic meaning leads to a new perspective on logic as well

### New logical notions

- Besides classical entailment, we get a notion of inquisitive entailment: φ inquisitively entails ψ iff whenever φ is resolved, ψ is resolved as well;
- We also get logical notions of relatedness. In particular, φ is a compliant response to ψ iff it addresses the issue raised by ψ without providing any redundant information.

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Note: classical notions are preserved; the logical agenda is extended, not revised (compare, e.g., with intuitionistic logic)

# **Pragmatics**

Pragmatics specifies how cooperative speakers should use the sentences of a language, given a particular context and the semantic meaning of those sentences

Classical (Gricean) pragmatics

- identifies semantic meaning with informative content
- is speaker-oriented
- Quality: say only what you believe to be true
- Quantity: be as informative as possible
- Relation: say only things that are relevant for the purposes of the conversation

# Inquisitive pragmatics

#### A new perspective

• Enriching the notion of semantic meaning leads to a new perspective on pragmatics as well

### Inquisitive pragmatics

- based on informative, but also inquisitive/attentive content
- speaker-oriented, but also hearer-oriented
- Sincerity: say only what you know, ask only what you want to know
- Transparency: publicly announce unacceptability of a proposal

- Quantity: say more, ask less
- Relation: be optimally compliant

## **Final remarks**

• Natural language semantics seeks to assign appropriate meanings to linguistic expressions in a systematic way



- Much work in inquisitive semantics so far has focussed on developing a richer space of meanings, and investigating the internal properties of these meanings, independently of the expressions in natural language that they may be assigned to
- This work establishes a framework for natural language semantics, but not really a theory of natural language

## Wh-questions

- To underline this point, consider the case of *wh*-questions
- Inquisitive semantics, qua framework, does not make any claims about the proper semantic analysis of *wh*-questions
- It offers a general framework to capture inquisitive content
- Hamblin's, Karttunen's, and Groenendijk & Stokhof's theories can all be expressed and compared in this framework
- The framework as such does not favor any of these theories

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• Indeed, combinations are also possible

### From framework to theory

- There is already some work connecting the new type of meanings with specific constructions in natural language
- However, much remains to be done on this front
- And this is exactly where the techniques developed in alternative semantics are bound to be extremely useful!

## Conclusion

- Inquisitive and alternative semantics are not notational variants or competing theories
- They are complementary efforts, using the same basic formal machinery, for very different purposes
- Alternative semantics offers an attractive compositional account of various constructions involving disjunction, indefinites, and indeterminate pronouns
- Inquisitive semantics offers a new notion of semantic meaning, that is intended to capture not only informative content, but also inquisitive and attentive content

# Thank you





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