## Logic and Conversation Assignment 3

Please return the assignment in pdf by email to: floris.roelofsen@gmail.com Due date: Monday 19/11

## **1** Inquisitive meanings

- 1. Prove that for any two propositions A and B:
  - $A \subseteq B$  if and only if
  - (i)  ${\cal A}$  is at least as informative as  ${\cal B}$  and
  - (ii) A is at least as inquisitive as the restriction of B to info(A).
- 2. Show that the notion of issues in lnqB is more general than the notion of issues in a partition semantics of questions such as the one employed in the Logic of Interrogation. That is, show (i) that every partition of a state s corresponds to an issue over s in the sense of lnqB, and (ii) that some issues over a state s in the sense of lnqB do not correspond to partitions.
- 3. Bonus: can you think of questions in natural language that express non-partitional issues?

## 2 Inquisitive algebra

- 1. Prove fact 6 in the lecture notes.
- 2. Prove fact 7 in the lecture notes.
- 3. For any set of states S, let  $S^{\downarrow}$  denote the downward closure of S, i.e.:

$$S^{\downarrow} = \{ s \mid s \subseteq s' \text{ for some } s' \in S \}$$

Suppose the set of all worlds is  $W = \{w_1, w_2, w_3, w_4\}$ , and let:

- $A = \{\{w_1, w_2\}\}^{\downarrow}$
- $B = \{\{w_1, w_3\}, \{w_2, w_4\}\}^{\downarrow}$

Compute  $A \Rightarrow B$ . Depict A, B, and  $A \Rightarrow B$  using the kind of pictures used in the lecture notes and in class. If you are using latex, you can find a template for drawing such pictures at:

https://sites.google.com/site/inquisitivesemantics/documents/pictures.tex